https://doi.org/10.15407/ujpe70.1.16

M.P. LIUL $^{1,\,2}$

¹ B. Verkin Institute for Low Temperature Physics and Engineering (*Kharkiv 61103, Ukraine*)

² Theoretical Quantum Physics Laboratory, Cluster for Pioneering Research (RIKEN, Wakoshi, Saitama, 351-0198, Japan; e-mail: liul@ilt.kharkov.ua)

INTERFEROMETRY AND DYNAMICS OF A TRANSMON-TYPE QUBIT IN FRONT OF A MIRROR

We will theoretically describe the stationary regime and coherent dynamics of a capacitively shunted transmon-type qubit which is placed in front of a mirror. The considered qubit is irradiated by two signals: pump (dressing) and probe. By changing the amplitudes and frequencies of these signals, we will study the system behavior. The main tool of our theoretical analysis is solving the Lindblad equation. We also discuss the transfer of Lindblad superoperators from the energy basis to the charge one. Theoretically obtained occupation probability is related to the experimentally measured value. This study helps to understand better the properties of qubit-mirror system and gives new insights about the underlying physical processes.

Keywords: transmon-type qubit, two-level quantum system, density matrix, Lindblad equation, quantum interference.

1. Introduction

Considerable attention is being drawn to topics related to quantum computing [1]. Among the promising building blocks for such devices, superconducting qubits stand out, operating on nanosecond scales with millisecond coherence times [2]. These qubits, controlled by microwaves and featuring lithographic scalability [3], hold a great potential for the advancement of quantum computers.

An essential aspect is the exploration of superconducting qubits within a semi-infinite transmission line [4], crucial for quantum electrodynamics, particularly waveguide quantum electrodynamics (WQED) [5]. Notably, in Ref. [6], it was revealed that a transmon qubit at the transmission line's end could amplify a probe signal with an amplitude gain of up to 7%. In comparison, single quantum dot [7] and natural atoms [8] exhibit much lower signal amplifications: 0.005% and 0.4%, respectively. Our investigation could address pertinent physics issues in WQED, including the dynamics in atom-like mirrors [9], collective Lamb shift [10], the dynamical Casimir effect [11], cross-Kerr effect [12], generation of nonclassical microwaves [13], probabilistic motional averaging [14], photon routing [15], and more.

Driven quantum systems find description through Landau–Zener–Stückelberg–Majorana (LZSM) transitions [16–18]. When driven periodically, these systems exhibit interference. LZSM interferometry, crucial for studying fundamental quantum phenomena and characterizing quantum systems, was explored in Refs. [16]. Additionally, quantum logic gates can be implemented using the LZSM dynamics [19].

This research is an extension of Ref. [20], where the developed theory was confirmed experimentally. In this article, we will build the dependences which were

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1

Citation: Liul M.P. Interferometry and dynamics of a transmon-type qubit in front of a mirror. *Ukr. J. Phys.* **70**, No. 1, 16 (2025). https://doi.org/10.15407/ujpe70.1.16.

[©] Publisher PH "Akademperiodyka" of the NAS of Ukraine, 2025. This is an open access article under the CC BY-NC-ND license (https://creativecommons.org/licenses/by-nc-nd/4.0/)

not considered before. The interferograms and dynamic plots presented in this paper allow one to understand better underlying physical processes and, thus, could be interesting and useful for setting up future experiments. In addition, we solve the Lindblad equation with Lindblad superoperators in different bases: a charge and an energy one. After comparison of obtained results with the experimental data, it was concluded that the superoperators have to be in the charge basis. This conclusion is intuitive, as the equation itself is formulated in this basis. Comparing the results obtained using Lindblad superoperators in different bases is crucial from a methodological perspective.

The rest of the paper is organized as follows. Section II describes the theoretical aspects of the research: the system Hamiltonian and the Lindblad master equation, which was used for obtaining the results, are introduced. In Sec. III, we study the relations between charge and energy bases. Section IV shows the obtained interferograms and Sec. V time dependencies. In Sec. VI, our conclusions are presented.

2. Theoretical Aspects

In the work [21], the experimentally studied reflection coefficient |r| is linked to the theoretically calculated an upper charge level $|1\rangle$ occupation probability P_1 . The authors stated that an increase in P_1 corresponds to a decrease in |r|. This relation can be explained in the following way. When the qubit is excited by the probe signal, it absorbs a portion of the signal's energy. This means that, in the case of the system's excitation, the reflection coefficient |r| decreases, while occupation probability P_1 increases. In that work, the computations were performed in the charge basis. In our analysis, we maintain this alignment between theoretical predictions and experimental results, conducting calculations in the charge basis. The transmon-type qubit which placed in front of a mirror can be characterized by the Hamiltonian:

$$H = -\frac{B_z}{2}\sigma_z - \frac{B_x}{2}\sigma_x,\tag{1}$$

where the diagonal part describes the energy-level modulation

$$B_z/\hbar = \omega_{10} + \delta \sin \omega_{\text{pump}} t, \qquad (2)$$

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1



Fig. 1. Conceptual sketch of the device. A two-level atom, point-like object (denoted by Q), is coupled to a semi-infinite transmission line waveguide. The atom is located away from the mirror (capacitance). A pump tone with frequency ω_{pump} is applied to modulate the transition frequency of the two-level atom. A weak probe tone with frequency ω_{p} is applied to the atom-mirror system to measure the reflection coefficient

the off-diagonal part corresponds to the coupling to the probe signal

$$B_x/\hbar = G\sin\omega_{\rm p}t.\tag{3}$$

To exclude the fast driving from the considered Hamiltonian the authors of Ref. [21] considered the unitary transformation $U = \exp(-i\omega_{\rm p}\sigma_z t/2)$ and the rotating-wave approximation [22] and, as a result, one obtained the new Hamiltonian

$$H_1 = -\frac{\hbar \Delta \omega}{2} \sigma_z + \frac{\hbar G}{2} \sigma_x, \qquad (4)$$

where

$$\widetilde{\Delta\omega} = \Delta\omega + f(t), \tag{5}$$

$$\Delta \omega = \omega_{\rm p} - \omega_{10}, \tag{6}$$

$$f(t) = \delta \sin \omega_{\text{pump}} t. \tag{7}$$

Here δ is the energy-level modulation amplitude, G describes the coupling to the probe signal (Rabi frequency of the probe signal). According to Ref. [21]

$$G = \frac{\omega_{\rm p} - \omega_{\rm node}}{\omega_{\rm node}} G_0, \tag{8}$$

where ω_{node} characterizes the qubit location in a semiinfinite transmission line (corresponding to the blue curve in Fig. 1), and G_0 is proportional to the probe signal amplitude. Moreover, we should mention that if $\omega_{\text{p}} = \omega_{\text{node}}$, the qubit is "hidden" or "decoupled" from the transmission line, with G = 0.

To describe the qubit dynamics, we utilize the Lindblad equation, which, in the charge basis with Hamiltonian (4), has the form:

$$\frac{d\rho}{dt} = -\frac{i}{\hbar} \left[\hat{H}_1, \rho \right] + \sum_{\alpha} \breve{L}_{\alpha} \left[\rho \right], \tag{9}$$

17



Fig. 2. Energy and charge states of a system as functions of $\Delta\omega$. The energy states $|E_{\rm down}\rangle$, $|E_{\rm up}\rangle$, which form the energy basis are indicated in orange and blue, respectively. The position of levels quasicrossing (anti-crossing), where the distance between levels is the smallest and equals to G is at the point $\Delta\omega = \Delta\omega^*$. After passing through this point, the charge states $|0\rangle$, $|1\rangle$, which form the charge basis, transfer to another curve. For example, going from the left to the right through the point $\Delta\omega = \Delta\omega^*$, the charge state $|0\rangle$ from the orange curve transfers to the blue one.

where $\rho = \begin{pmatrix} \rho_{00} & \rho_{01} \\ \rho_{01}^* & 1 - \rho_{00} \end{pmatrix}$ is the density matrix, such that $P_1 = 1 - \rho_{00}$. The Lindblad superoperator \breve{L}_{α} describes the system relaxation induced by interactions with the environment,

$$\breve{L}_{\alpha}\left[\rho\right] = L_{\alpha}\rho L_{\alpha}^{+} - \frac{1}{2}\left\{L_{\alpha}^{+}L_{\alpha},\rho\right\},\tag{10}$$

where $\{a, b\} = ab + ba$ is the anticommutator. For a qubit, there exist two relaxation channels: dephasing (described by L_{ϕ}) and energy relaxation (described by L_{relax}). In the energy basis, the corresponding operators can be expressed in the following form:

$$L_{\rm relax}^{\rm energy} = \sqrt{\Gamma_1}\sigma^+, \quad L_{\phi}^{\rm energy} = \sqrt{\frac{\Gamma_{\phi}}{2}}\sigma_z,$$
 (11)

with $\sigma^+ = \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$, $\sigma_z = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$, Γ_1 being the qubit relaxation, $\Gamma_2 = \Gamma_1/2 + \Gamma_{\phi}$ is the decoherence rate, Γ_{ϕ} is the pure dephasing rate.

3. Energy and Charge Bases

In this section, we will discuss the question related to the selection of an appropriate basis. As it was mentioned, the Hamiltonian (4) and the Lindlad equation (9) were written in a charge basis, while the relaxations Γ_1 and Γ_{ϕ} are determined in the energy basis. So, one should transfer Lindblad operators from the energy basis to the charge one. To study this question, let us rewrite Hamiltonian (4) in the form:

$$H(t) = H_0 + V(t),$$
(12)

where the constant component is equal to

$$H_0 = \frac{\hbar G}{2} \sigma_x - \frac{\hbar}{2} \left(\omega_{\rm p} - \omega_{10} \right) \sigma_z = \frac{\hbar G}{2} \sigma_x - \frac{\hbar}{2} \Delta \omega \sigma_z,$$
(13)

and time-dependent part can be written as

$$V(t) = -\frac{\hbar}{2} \,\delta \sin \omega_{\text{pump}} \, t \sigma_z. \tag{14}$$

In other words, Hamiltonian (4) can be considered as an effective Hamiltonian of a two-level system with tunneling amplitude G, and excitation h(t) = $= -\frac{\hbar}{2} (\Delta \omega + \delta \sin \omega_{\text{pump}} t).$

The transfer matrix which provides transfer from a charge basis to an energy one has a form:

$$S = \begin{pmatrix} \gamma_+ & \gamma_-\\ \gamma_- & -\gamma_+ \end{pmatrix},\tag{15}$$

where

$$\gamma_{\pm}(t) = \frac{1}{\sqrt{2}} \sqrt{1 \pm \frac{\Delta\omega}{\sqrt{\Delta\omega^2 + G^2}}}.$$
(16)

The matrix S diagonalizes time-independent part of the Hamiltonian H_0 (13):

$$S^{\dagger}H_0S = H'_0 = \begin{pmatrix} E_{\rm down} & 0\\ 0 & E_{\rm up} \end{pmatrix},\tag{17}$$

where E_{down} , E_{up} – are eigenvalues of the Hamiltonian H_0 . The expressions for the lower energy level E_{down} and the upper energy level E_{up} have the following form:

$$E_{\rm down} = -\frac{1}{2}\sqrt{\Delta\omega^2 + G^2},\tag{18}$$

$$E_{\rm up} = \frac{1}{2}\sqrt{\Delta\omega^2 + G^2}.$$
(19)

The corresponding energy states $|E_{\rm down}\rangle$, $|E_{\rm up}\rangle$ as functions of $\Delta\omega$ are depicted in Fig. 2. Figure 2 also shows for the dependence of charge states $|0\rangle$, $|1\rangle$ on $\Delta\omega$.

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1

18

Therefore, one can transfer Lindblad superoperators $L_{\alpha}^{\text{energy}}$ from energy basis to the charge one L_{α} by using the relation:

$$L_{\alpha} = SL_{\alpha}^{\text{energy}}S^{\dagger}.$$
 (20)

Substitution of Eqs. (11, 20) to the Lindblad equation (9) will give the necessary dependence $P_1 = P_1(t)$, which is used for building theoretical plots.

4. Qubit Interferometry

By solving Eq. (9), we get P_1 as a function of time t, the pump frequency ω_{pump} , the pump amplitude δ , the probe frequency ω_{p} , the signal amplitude G. The occupation probability of the upper charge level is a function of all these parameters, $P_1 =$ $= P_1(t, \omega_{\text{pump}}, \omega_{\text{p}}, \delta, G)$. We can also calculate the dependencies for P_1 in the stationary regime by averaging the results over time.

To obtain the time-averaged values, we analyzed the curve $P_1 = P_1(t)$ to select the minimum time t_{\min} after which the amplitude of oscillations does not change. Then averaging was applied for the interval $[t_{\min}, t_{\text{final}}]$, where t_{final} corresponds to the pulse off time. We determined that, in our case, $t_{\min} = 1.5 \ \mu \text{s}$ and $t_{\text{final}} = 2.0 \ \mu \text{s}$ (see Ref. [20] for more details).

In this section, we theoretically investigate the dependence of the qubit upper charge level occupation probability P_1 on the pump frequency ω_{pump} and the probe frequency ω_{p} . Note that the experimental study of such dependence was not conducted. But since the values of the fitting parameters were found in Ref. [20], we can construct such a dependence. It is shown in Fig. 3, *a* corresponds to the pump amplitude $\delta = [10]$ MHz, for (*b*) the pump amplitude is equal to $\delta = [20]$ MHz. From the analysis of interferograms, it becomes clear that the larger the pumping amplitude δ , the larger the amplitude along the ω_{p} axis. Similar dependencies can be observed in Ref. [21], where only the stationary case was considered.

Such interferograms are useful not only for obtaining fitting parameters between theory and experiment, but they also play a key role in system characterization. In particular, they can help to:

• estimate the system decoherence time;

• provide a tool for calibrating signal strength during experimental studies;

• open up new possibilities for multiphoton spectroscopy.

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1

5. Qubit Dynamics

5.1. Dependence of the upper charge level occupation probability on the probe frequency in the case of Lindblad operators in the energy basis

This section presents the results of calculations [n the case of Lindblad operators in the energy basis. Note that this approach is not correct and the obtained theoretical dependencies are not consistent with the experimental ones. However, from a methodological point of view, it is useful to give such an example. Figure 4 shows the pictures obtained as a result of such calculations. This dependence corresponds to Fig. 4, d-f in Ref. [20].

From the comparison of the theoretical (Fig. 4, a-c in c) and the corresponding experimental (Fig. 4, a-c in Ref. [20]) pictures, we can conclude that the Lindblad operators have to be transferred to the charge basis. The obtained dependencies have a behavior similar to the experimental ones, for example, resonances occur at $\Delta \omega = k \omega_{\text{pump}}$ both in the theory and in the experiment. However, unlike the experimental ones, in the theoretical pictures, the resonance k = 0 is slightly shifted from the line $\omega_p/2\pi = [5]$ GHz, and it is more blurred (wider).

5.2. Dependence of the upper charge level occupation probability on the probe frequency and time

In the presented section, we will construct dependencies similar to those shown in the work [20] in



Fig. 3. LZSM interferograms. The upper charge level occupation probability P_1 as a function of the pump frequency ω_{pump} and the probe frequency ω_{p} at a fixed pump amplitude δ for $G(\omega_{\text{p}}/2\pi = 5 \text{ GHz}) = 2\pi \times 0.7 \text{ MHz}$. Corresponds to the pump amplitude value $\delta = [10]$ MHz (a), for the pump amplitude value is $\delta = [20]$ MHz (b)



Fig. 4. Calculated dynamics of a transmon-type qubit with Lindblad operators in the energy basis. Dependence of the upper charge level occupation probability P_1 on time t and the probe frequency ω_p at different pump frequencies ω_{pump} . During the calculations, the following values were used: the probe amplitude $G(\omega_p/2\pi = 5 \text{ GHz}) = 2\pi \times 1.4 \text{ MHz}$, the pump amplitude $\delta = [10]$ MHz. (a, b, c) show plots constructed from data calculated theoretically in the case of Lindblad operators in the energy basis. The qubit is irradiated with a pump frequency of (a) $\omega_{pump}/2\pi = [5]$ MHz, (b) $\omega_{pump}/2\pi = [10]$ MHz, (c) $\omega_{pump}/2\pi = [15]$ MHz



Fig. 5. Coherent dynamics of a transmon-type qubit at low frequencies of the ω_{pump} pump signal. The upper charge level occupation probability P_1 as a function of time t and the probe frequency ω_p at different pump frequencies ω_{pump} . The following parameter values were used for the calculations: amplitude of the probe signal $G(\omega_p/2\pi = 5 \text{ GHz}) = 2\pi \times 1.4 \text{ MHz}$, amplitude of the pump signal $\delta = [10]$ MHz. The qubit is irradiated by pump signal with a frequency of (a) $\omega_{\text{pump}}/2\pi = [1]$ MHz, (b) $\omega_{\text{pump}}/2\pi = [2]$ MHz, (c) $\omega_{\text{pump}}/2\pi = [3]$ MHz

Fig. 4, d-f, but at lower values of the frequency of the pump signal ω_{pump} . Figure 5 shows the obtained interferograms. The qubit is irradiated by pump signal with a frequency of (a) $\omega_{\text{pump}}/2\pi = [1]$ MHz, (b) $\omega_{\text{pump}}/2\pi = [2]$ MHz, (c) $\omega_{\text{pump}}/2\pi = [3]$ MHz.

In Fig. 5, *a*, in the case $\omega_{\text{pump}}/2\pi = [1]$ MHz, one would expect resonances at the distance $\Delta\omega/2\pi =$ = [1] MHz to each other along the ω_{p} axis, but such behavior is not observed. This, most likely, is due to the fact that the resonance peaks are located too close to each other and therefore merge. For the Fig. 5, *b*, strong peaks are observed only at a distance $\omega/2\pi = [8]$ MHz from the line $\omega_{\text{p}}/2\pi = [5]$ GHz, for the Fig. 5, *c* strong peaks are observed only at a distance $\omega/2\pi = [6]$ MHz, [9] MHz from the line $\omega_{\rm p}/2\pi = [5]$ GHz, while peaks at a distance of $\omega/2\pi = [3]$ MHz are weakly highlighted.

5.3. Dependence of the upper charge level occupation probability on the probe amplitude and the probe frequency for at different values of the probe amplitude and the relaxation rate

In the presented section, we will investigate the dependence of the upper charge level occupation probability on time t and the probe frequency $\omega_{\rm p}$ at different values of the probe amplitude G and the relaxation rate Γ_1 for the pump frequency $\omega_{\rm pump}/2\pi =$ = [5] MHz. For calculations, the pump amplitude is

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1



Fig. 6. Dependence of the upper charge level occupation probability on time t and the probe frequency $\omega_{\rm p}$ at different values of the probe amplitude G and the relaxation rate Γ_1 for the pump frequency $\omega_{\rm pump}/2\pi = [5]$ MHz. For calculations, the value of the pump amplitude was taken equal to $\delta = [10]$ MHz. The values of the probe amplitude G change from left to right and have the values $G/2\pi = [0.7]$ MHz, $G/2\pi = [1.4]$ MHz, $G/2\pi = [2.8]$ MHz. The relaxation rate changes from top to bottom and has the value $\Gamma_1 = [0.14]$ MHz, $\Gamma_1 = [0.28]$ MHz, $\Gamma_1 = [1.12]$ MHz respectively

taken equal to $\delta = [10]$ MHz. The resulting dependencies are shown in Fig. 6.

By analyzing the obtained dependencies, we can draw several conclusions. As the relaxation rate Γ_1 increases while keeping the probe amplitude G (within a certain column we move from top to bottom), the resonances become less blurred. With increasing the relaxation rate Γ_1 , the occupation probability P_1 decreases. These facts are understandable, because with an increase in the relaxation rate, the system faster relaxes to the unexcited state, what is observed on the obtained dependencies.

In the case $G/2\pi = [2.8]$ MHz, the first resonances observed at $t \approx 0.25 \ \mu$ s are clearly expressed, while for probe amplitude $G/2\pi = [1.4]$ MHz. The maximum value of the upper charge level occupation probability P_1 corresponds to the second and third resonances, while the first resonance is weakly high-

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1

lighted. For $G/2\pi = [0.7]$ MHz and $\Gamma_1 = [0.14]MHz$, $\Gamma_1 = [0.28]$ MHz during the first $t \approx 1 \ \mu$ s the value of the upper charge level occupation probability P_1 has smaller values than for longer time values. In the case where $G/2\pi = [0.7]$ MHz and $\Gamma_1 = [1.12]$ MHz, the first two resonances ($t < 0.5 \ \mu$ s) are highlighted more weakly than the following ones.

6. Conclusions

We considered the dynamics and stationary mode of a transmon-type capacitive shunted qubit in front of a mirror, which is affected by two signals: probing and pumping.

To analyze the steady state, the upper charge level occupation probability P_1 was calculated as a function of the pump frequency ω_{pump} and the probe frequency ω_{p} at the fixed pump amplitude δ and the probe amplitude G. The resulting dependencies can be used to obtain fitting parameters; system decoherence time estimation; power calibration; studying multiphoton spectroscopy.

To analyze the dynamics, we plotted the dependencies of the upper charge level occupation probability P_1 on (a) time t and the probe frequency $\omega_{\rm p}$ at different pump frequencies $\omega_{\rm pump}$; (b) time t and the probe frequency $\omega_{\rm p}$ at different values of the probe amplitude G and the relaxation rate Γ_1 for the pump frequency $\omega_{\rm pump}/2\pi = [5]MHz$. The obtained results can be used in setting up future experiments.

The Lindblad equation with Lindblad superoperators in different bases: a charge and an energy one was solved. One concluded that the superoperators had to be in the charge basis, since the equation is also written in this basis. Such a comparison should be useful from the methodological point of view.

The author acknowledge fruitful discussions with S.N. Shevchenko, A.I. Ryzhov, O.V. Ivakhnenko. The author was partially supported by the grant from the National Academy of Sciences of Ukraine for research works of young scientists (1/H-2023, 0123U103073).

- M.A. Nielsen, I.L. Chuang. Quantum Computation and Quantum Information: 10th Anniversary Edition (Cambridge University Press, 2010).
- A.F. Kockum, F. Nori. Quantum bits with Josephson junctions. In: Fundamentals and Frontiers of the Josephson Effect (Springer International Publishing, 2019).
- W.D. Oliver, P.B. Welander. Materials in superconducting quantum bits. MRS Bulletin 38, 816 (2013).
- I.-C. Hoi, A.F. Kockum, L. Tornberg, A. Pourkabirian, G. Johansson, P. Delsing, C.M. Wilson. Probing the quantum vacuum with an artificial atom in front of a mirror. *Nat. Phys.* **11**, 1045 (2015). arXiv:1410.8840v1 [quant-ph].
- B. Kannan, M.J. Ruckriegel, D.L. Campbell, A.F. Kockum, J. Braumuller, D.K. Kim, M. Kjaergaard, P. Krantz, A. Melville, B.M. Niedzielski, A. Vepsalainen, R. Winik, J.L. Yoder, F. Nori, T.P. Orlando, S. Gustavsson, W.D. Oliver. Waveguide quantum electrodynamics with superconducting artificial giant atoms. *Nature* 583, 775 (2020). arXiv:1912.12233v3 [quant-ph].
- P.Y. Wen, A.F. Kockum, H. Ian, J.C. Chen, F. Nori, I.-C. Hoi. Reflective amplification without population inversion from a strongly driven superconducting qubit. *Phys. Rev. Lett.* **120**, 063603 (2018).
- X. Xu, B. Sun, P.R. Berman, D.G. Steel, A.S. Bracker, D. Gammon, L.J. Sham. Coherent optical spectroscopy of a strongly driven quantum dot. *Science* **317**, 929 (2007).

- F.Y. Wu, S. Ezekiel, M. Ducloy, B.R. Mollow. Observation of amplification in a strongly driven two-level atomic system at optical frequencies. *Phys. Rev. Lett.* 38, 1077 (1977).
- M. Mirhosseini, E. Kim, X. Zhang, A. Sipahigil, P.B. Dieterle, A.J. Keller, A. Asenjo-Garcia, D.E. Chang, O. Painter. Cavity quantum electrodynamics with atomlike mirrors. *Nature* 569, 692 (2019).
- P.Y. Wen, K.-T. Lin, A.F. Kockum, B. Suri, H. Ian, J.C. Chen, S.Y. Mao, C.C. Chiu, P. Delsing, F. Nori, G.-D. Lin, I.-C. Hoi. Large collective Lamb shift of two distant superconducting artificial atoms. *Phys. Rev. Lett.* **123**, 233602 (2019).
- C.M. Wilson, G. Johansson, A. Pourkabirian, M. Simoen, J.R. Johansson, T. Duty, F. Nori, P. Delsing. Observation of the dynamical Casimir effect in a superconducting circuit. Nature 479, 376 (2011).
- I.-C. Hoi, A.F. Kockum, T. Palomaki, T.M. Stace, B. Fan, L. Tornberg, S.R. Sathyamoorthy, G. Johansson, P. Delsing, C.M. Wilson. Giant Cross-Kerr effect for propagating microwaves induced by an artificial atom. *Phys. Rev. Lett.* **111**, 053601 (2013).
- I.-C. Hoi, T. Palomaki, J. Lindkvist, G. Johansson, P. Delsing, C.M. Wilson. Generation of nonclassical microwave states using an artificial atom in 1D open space. *Phys. Rev. Lett.* **108**, 263601 (2012).
- D. Karpov, V. Monarkha, D. Szombati, A. Frieiro, A. Omelyanchouk, E. Il'ichev, A. Fedorov, S. Shevchenko. Probabilistic motional averaging. *Eur. Phys. J. B* 93, 49 (2020).
- I.-C. Hoi, C.M. Wilson, G. Johansson, T. Palomaki, B. Peropadre, P. Delsing. Demonstration of a singlephoton router in the microwave regime. *Phys. Rev. Lett.* **107**, 073601 (2011).
- O.V. Ivakhnenko, S.N. Shevchenko, F. Nori. Nonadiabatic Landau–Zener–Stuckelberg–Majorana transitions, dynamics and interference. *Phys. Rep.* 995, 1 (2023).
- S.N. Shevchenko. Mesoscopic Physics meets Quantum Engineering (World Scientific, 2019).
- M.P. Liul, A.I. Ryzhov, S.N. Shevchenko. Rate equation approach for a charge qudit. *Eur. Phys. J.: Spec. Top.* (2023).
- D.L. Campbell, Y.-P.Shim, B. Kannan, R. Winik, D.K. Kim, A. Melville, B.M. Niedzielski, J.L. Yoder, C. Tahan, S. Gustavsson, W.D. Oliver. Universal nonadiabatic control of small-gap superconducting qubits. *Phys. Rev. X* 10, 041051 (2020).
- M.P. Liul, C.-H. Chien, C.-Y. Chen, P.Y. Wen, J.C. Chen, Y.-H. Lin, S.N. Shevchenko, F. Nori, I.-C. Hoi. Coherent dynamics of a photon-dressed qubit. *Phys. Rev. B* 107, 195441 (2023).
- P.Y. Wen, O.V. Ivakhnenko, M.A. Nakonechnyi, B. Suri, J.-J. Lin, W.-J. Lin, J.C. Chen, S.N. Shevchenko, F. Nori, I.-C. Hoi. Landau–Zener–Stuckelberg–Majorana interferometry of a superconducting qubit in front of a mirror. *Phys. Rev. B* **102**, 075448 (2020).

ISSN 2071-0194. Ukr. J. Phys. 2025. Vol. 70, No. 1

 M. Silveri, K. Kumar, J. Tuorila, J. Li, A. Vepsalainen, E. Thuneberg, G. Paraoanu. Stueckelberg interference in a superconducting qubit under periodic latching modulation. *New J. Phys.* 17, 043058 (2015). Received 26.06.24

М.П. Люль

ІНТЕРФЕРОМЕТРІЯ ТА ДИНАМІКА КУБІТА ТИПУ ТРАНСМОН, РОЗМІЩЕНОГО ПЕРЕД ДЗЕРКАЛОМ

Ми теоретично описуємо стаціонарний режим і когерентну динаміку ємнісно шунтованого кубіта типу трансмон, який розміщено перед дзеркалом. Розглянутий кубіт опромінюється двома сигналами: збуджуючим і зондуючим. Змінюючи амплітуди та частоти цих сигналів, ми вивчаємо поведінку системи. Основним інструментом нашого теоретичного аналізу є розв'язування рівняння Ліндблада. Також ми обговорюємо переведення супероператорів Ліндблада з енергетичного базису на зарядовий. Теоретично отримана ймовірність заселеності має відношення до експериментально виміряного значення. Представлене дослідження допомагає краще зрозуміти властивості системи кубіт-дзеркало та пропонує новий погляд на основні фізичні явища та процеси, які в ній відбуваються.

Ключові слова: кубіт типу трансмон, дворівнева квантова система, матриця густини, рівняння Ліндблада, квантова інтерференція.